

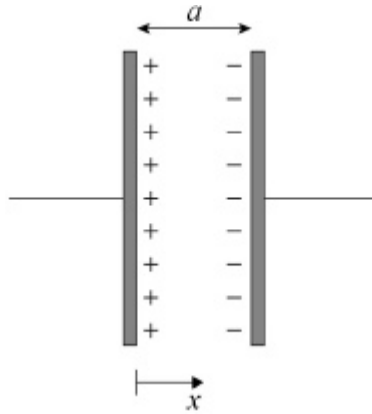
# A LEVEL PHYSICS

## WORKED SOLUTIONS

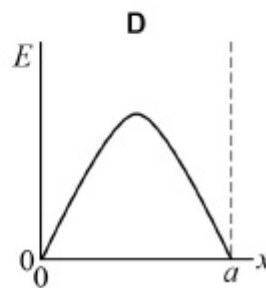
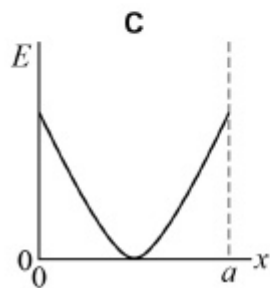
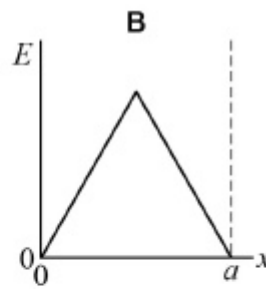
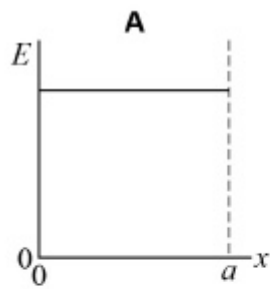
### 7.3. Electric Fields MCQ



1. Two parallel metal plates of separation  $a$  carry equal and opposite charges.



Which graph best represents how the electric field strength  $E$  varies with the distance  $x$  in the space between the two plates?



- A
- B
- C
- D

*Electric field is constant*

(Total 1 mark)

2. A particle of mass  $m$  and charge  $q$  is accelerated through a potential difference  $V$  over a distance  $d$ .

What is the average acceleration of the particle?

- A   $\frac{qV}{md}$
- B   $\frac{mV}{qd}$
- C   $\frac{V}{mqd}$
- D   $\frac{dV}{mq}$

$$F = ma \quad F = \frac{E}{d} = \frac{Vq}{d}$$

$$ma = \frac{Vq}{d}$$

$$a = \frac{Vq}{md}$$

(Total 1 mark)

3. An electron on the surface of the Earth is placed in an electric field of strength  $5000 \text{ N C}^{-1}$ .

What is  $\left(\frac{\text{electric force}}{\text{gravitational force}}\right)$  for the electron?

- A   $1.1 \times 10^{-14}$
- B   $2.9 \times 10^{-10}$
- C   $3.4 \times 10^9$
- D   $9.0 \times 10^{13}$

$$\frac{F_E}{F_g} = \frac{QE}{(GmM/r^2)} = \frac{QE r^2}{GmM}$$

$$\frac{F_E}{F_g} = \frac{1.60 \times 10^{-19} \times 5000 \times (6.37 \times 10^6)^2}{6.67 \times 10^{-11} \times 9.11 \times 10^{-31} \times 5.97 \times 10^{24}}$$

$$= 9.02 \times 10^{13}$$

(Total 1 mark)

4. An  $\alpha$  particle makes a head-on collision with a gold nucleus containing 79 protons. The distance of closest approach of the  $\alpha$  particle to the nucleus is  $4.0 \times 10^{-14} \text{ m}$ .

What electrostatic force acts on the gold nucleus when at this separation?

- A   $9.1 \times 10^{-11} \text{ N}$
- B   $23 \text{ N}$
- C   $290 \text{ N}$
- D   $1.4 \times 10^{20} \text{ N}$

$$F = \frac{Q_1 Q_2}{4\pi \epsilon_0 r^2}$$

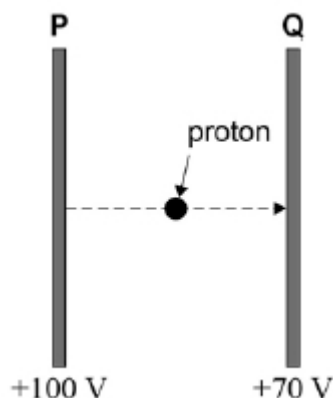
$$F = \frac{2 \times 79 \times (1.60 \times 10^{-19})^2}{4 \times \pi \times 8.85 \times 10^{-12} \times (4.0 \times 10^{-14})^2}$$

$$F = 22.7 \text{ N}$$

(Total 1 mark)

5. Two fixed parallel metal plates **P** and **Q** are at constant electrical potentials of +100 V and +70 V respectively. A proton travelling from **P** to **Q** experiences a force  $F$  due to the electric field between **P** and **Q**, and a change of potential energy of  $\Delta E_p$ .

Force in opposite direction to  $E_p$  gain



$$\begin{aligned} \Delta E_p &= E_Q - E_P \\ &= 70\text{eV} - 100\text{eV} \\ &= -30\text{eV} \end{aligned}$$

Which line, **A** to **B**, in the table gives the direction of  $F$  and the value of  $\Delta E_p$ ?

	Direction of $F$	$\Delta E_p$	
<b>A</b>	towards <del>P</del>	+30 <del>eV</del>	<input type="radio"/>
<b>B</b>	towards <b>Q</b>	+30 <del>eV</del>	<input type="radio"/>
<b>C</b>	towards <b>Q</b>	-30 eV	<input checked="" type="radio"/>
<b>D</b>	towards <del>P</del>	-30 eV	<input type="radio"/>

(Total 1 mark)

6. An electron moves through a distance of 0.10 m parallel to the field lines of a uniform electric field of strength 2.0 kN C<sup>-1</sup>.

What is the work done on the electron?

- A** zero
- B**  $1.6 \times 10^{-17}$  J
- C**  $3.2 \times 10^{-17}$  J
- D**  $1.6 \times 10^{-21}$  J

$$W = Fs \quad F = EQ$$

$$W = EQs$$

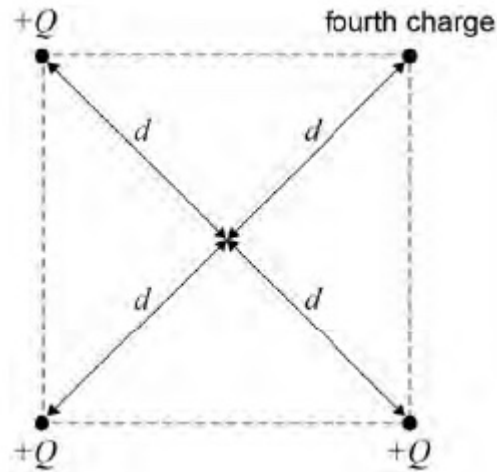
$$W = 2000 \times 1.60 \times 10^{-19} \times 0.10$$

$$W = 3.2 \times 10^{-17} \text{ J}$$

(Total 1 mark)

7.

Four positive charges are fixed at the corners of a square as shown.



The total potential at the centre of the square, a distance  $d$  from each charge, is  $\frac{5Q}{4\pi\epsilon_0 d}$

Three of the charges have a charge of  $+Q$

What is the magnitude of the fourth charge?

A  $-\frac{7Q}{4}$

B  $Q$

C  $\sqrt{2}Q$

D  $2Q$

$$V = \frac{Q}{4\pi\epsilon_0 d}$$

$$V_T = \frac{\sum Q}{4\pi\epsilon_0 d} = \frac{5Q}{4\pi\epsilon_0 d}$$

$$\sum Q = 5Q$$

$$4^{\text{th}} \text{ charge} = 5Q - Q - Q - Q = 2Q$$

(Total 1 mark)

8.

A charged spherical conductor has a radius  $r$ . An electric field of strength  $E$  exists at the surface due to the charge.

What is the potential of the spherical conductor?

A  $r^2 E$

B  $r E^2$

C  $\frac{E}{r}$

D  $r E$

$$E = \frac{V}{d}$$

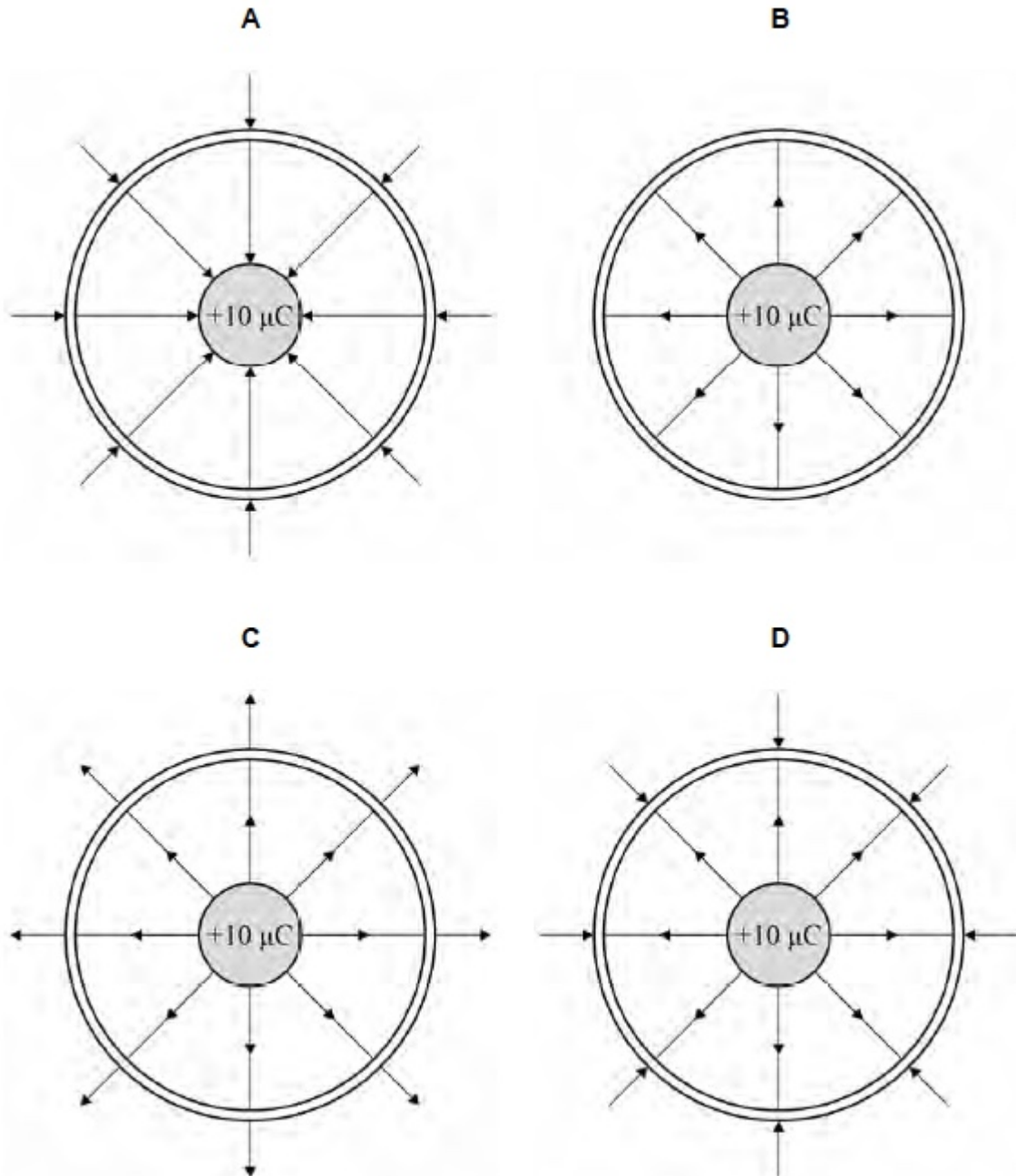
$$V = Ed = rE$$

(Total 1 mark)

9.

A conducting sphere holding a charge of  $+10 \mu\text{C}$  is placed centrally inside a second uncharged conducting sphere.

Which diagram shows the electric field lines for the system?



- A
- B
- C
- D

*+ve charge ∴ radial field  
lines point outwards  
uncharged conducting sphere becomes charged,  
acts as a positively charged sphere  
∴ lines in the same direction*

(Total 1 mark)

10. The ionisation potential for the atoms of a gas is  $V$ . Electrons of mass  $m$  and charge  $e$  travelling at a speed  $v$  can just cause ionisation of atoms in the gas.

What is  $V$ ? *Mean to be a lowercase 'v'*

A  $\frac{eV}{2m}$

B  $\frac{2eV}{m}$

C  $\sqrt{\frac{eV}{2m}}$

D  $\sqrt{\frac{2eV}{m}}$

$V = \frac{E_k}{Q}$  *Work done on atoms by electrons*

$V = \frac{\frac{1}{2}mv^2}{e}$

$2eV = mv^2$

$v = \sqrt{\frac{2eV}{m}}$

(Total 1 mark)

11. An electric field acts into the plane of the paper. An electron enters the field at  $90^\circ$  to the field lines.

The force on the electron is

A zero.

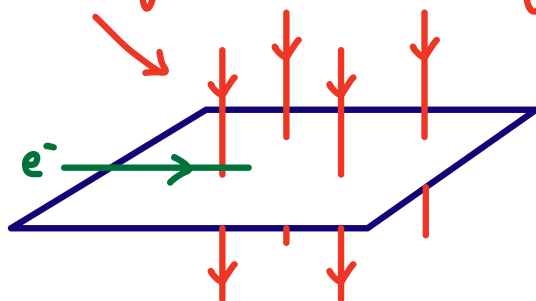
B along the direction of the field.

C at  $90^\circ$  to the field.

D opposite to the direction of the field.

(Total 1 mark)

*Direction = force on a +ve charge*



*∴ force on -ve electron must be opposite i.e. up out of paper*

**12.**

A positive charge of  $2.0 \times 10^{-4}$  C is placed in an electric field at a point where the potential is +500 V.

What is the potential energy of the system?

A  $1.0 \times 10^{-1}$  J



B  $1.0 \times 10^{-1}$  J C<sup>-1</sup>



C  $4.0 \times 10^{-7}$  J



D  $4.0 \times 10^{-7}$  J C<sup>-1</sup>

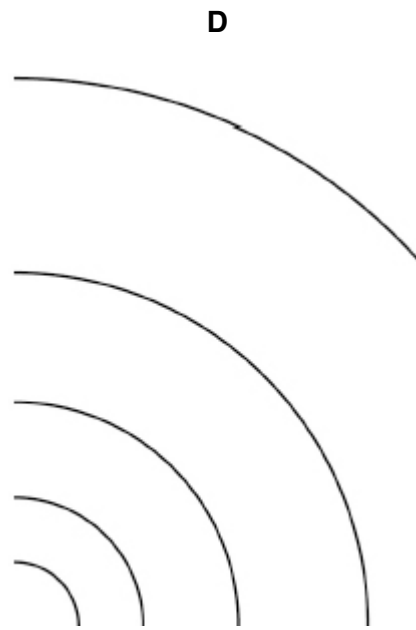
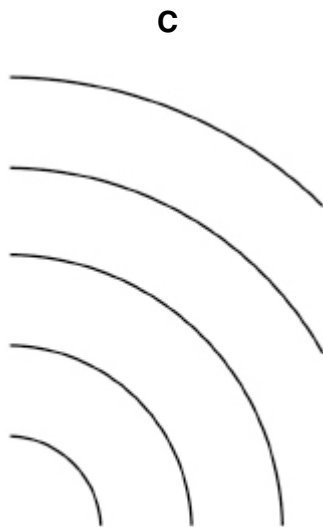
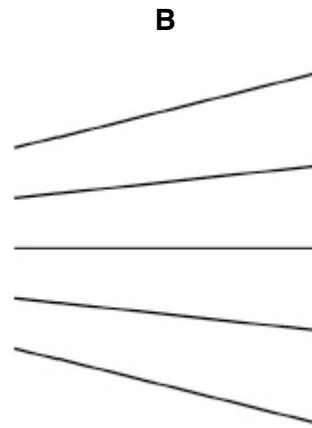
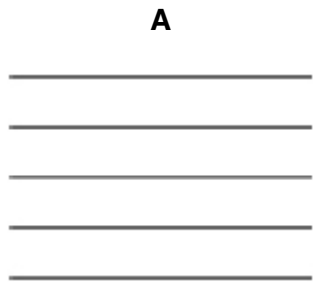


$$\begin{aligned} E_p &= QV \\ &= 2.0 \times 10^{-4} \times 500 \\ &= 1.0 \times 10^{-1} \text{ J} \end{aligned}$$

(Total 1 mark)



13. Which diagram shows lines of equipotential in steps of equal potential difference near an isolated point charge?



A

B

C

D

$V \propto \frac{1}{r}$   $\therefore$  must be parallel, concentric circles that get more spaced out

(Total 1 mark)

14. Two fixed charges of magnitude  $+Q$  and  $+3Q$  repel each other with a force  $F$ . An additional charge of  $-2Q$  is given to each charge.

What are the magnitude and the direction of the force between the charges?

	Magnitude of force	Direction of force
A	$\frac{F}{3}$	<del>repulsive</del>
B	<del><math>5F</math></del>	attractive
C	<del><math>5F</math></del>	<del>repulsive</del>
<u>D</u>	$\frac{F}{3}$	attractive





$$F \propto Q_1 Q_2$$

$$F_1 = +Q \cdot +3Q = 3Q^2$$

$$F_2 = -Q \cdot +Q = -Q^2$$

$$F_2 = -\frac{F_1}{3}$$

(Total 1 mark)

15. At a distance  $L$  from a fixed point charge, the electric field strength is  $E$  and the electric potential is  $V$ .

What are the electric field strength and the electric potential at a distance  $3L$  from the charge?

	Electric field strength	Electric potential
A	<del><math>\frac{E}{3}</math></del>	<del><math>\frac{V}{9}</math></del>
B	<del><math>\frac{E}{3}</math></del>	$\frac{V}{3}$
<u>C</u>	$\frac{E}{9}$	$\frac{V}{3}$
D	$\frac{E}{9}$	<del><math>\frac{V}{9}</math></del>





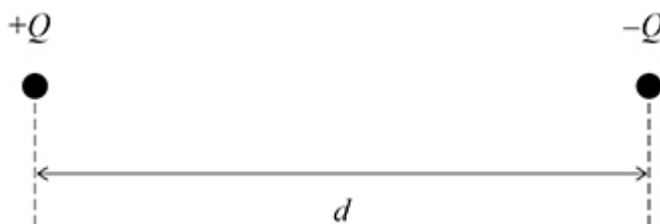
(Total 1 mark)

$$E \propto \frac{1}{r^2} \quad \therefore \frac{E}{3^2} = \frac{E}{9}$$

$$V \propto \frac{1}{r} \quad \therefore \frac{V}{3} = \frac{V}{3}$$

16. The diagram shows a particle with charge  $+Q$  and a particle with charge  $-Q$  separated by a distance  $d$ .

The particles exert a force  $F$  on each other.



An additional charge of  $+2Q$  is then given to each particle and their separation is increased to  $2d$ .

What is the force that now acts between the particles?

A an attractive force of  $\frac{9}{2}F$

B an attractive force of  $\frac{9}{4}F$

C a repulsive force of  $\frac{3}{2}F$

D a repulsive force of  $\frac{3}{4}F$

$$F \propto Q_1 Q_2 / d^2$$

$$F_1 = +Q \cdot -Q / d^2 = -Q^2 / d^2$$

$$F_2 = +3Q \cdot +Q / (2d)^2 = +\frac{3Q^2}{4d^2}$$

(Total 1 mark)

17. Two protons are separated by distance  $r$ . The electrostatic force between the two protons is  $X$  times the gravitational force between them.

What is the best estimate for  $X$ ?

A  $10^{20}$

B  $10^{28}$

C  $10^{36}$

D  $10^{42}$

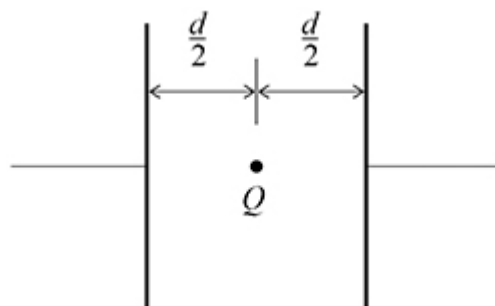
$$F_g = \frac{10^{-11} \times (10^{-27})^2}{r^2} \approx \frac{10^{-65}}{r^2}$$

$$F_E = \frac{(10^{-19})^2}{10 \times 10 \times 10^{-12} r^2} = \frac{10^{-28}}{r^2}$$

(Total 1 mark)

$$F_E / F_g = \frac{10^{-28}}{10^{-65}} \approx 10^{37} \text{ (very rough)}$$

18. Two parallel metal plates separated by a distance  $d$  have a potential difference  $V$  across them. A particle with charge  $Q$  is placed midway between the plates.



What is the magnitude of the electrostatic force acting on the particle?

- A zero
- B  $\frac{QV}{2d}$
- C  $\frac{QV}{d}$
- D  $\frac{2QV}{d}$

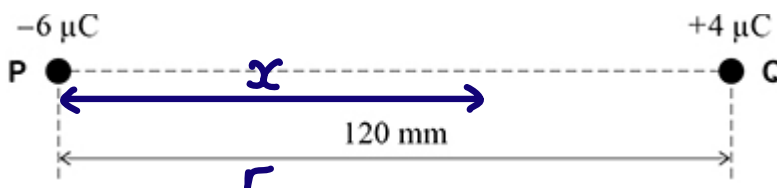
Handwritten notes:

$$F = EQ \quad E = \frac{V}{d}$$

$$F = \frac{VQ}{d}$$

(Total 1 mark)

19. Two charged particles P and Q are separated by a distance of 120 mm. X is a point on the line between P and Q where the electric potential is zero.



What is the distance from P to X?

- A 40 mm
- B 48 mm
- C 60 mm
- D 72 mm

Handwritten notes:

$$V \propto \frac{Q}{r} \quad V_P + V_Q = 0 \quad V_P = -V_Q$$

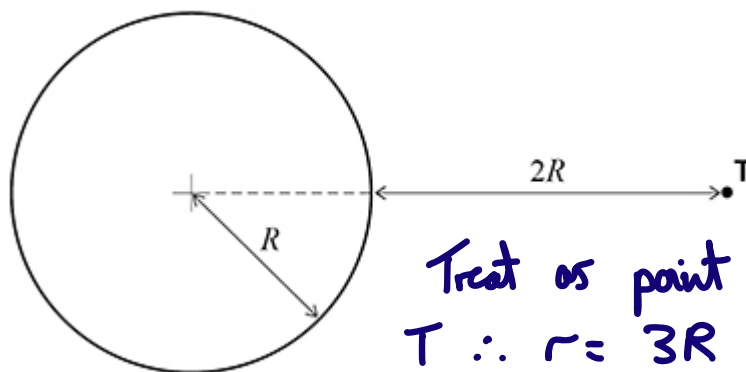
$$\frac{Q_P}{x} = \frac{-Q_Q}{r-x} \quad Q_P r - Q_P x = -Q_Q x$$

$$x(Q_P - Q_Q) = Q_P r$$

$$x = \frac{-6 \times 120}{-6 - 4} = \frac{720}{10} = 72 \text{ mm}$$

(Total 1 mark)

20. An isolated spherical conductor is charged. The conductor has a radius  $R$  and an electric potential  $V$ . The electric field strength at its surface is  $E$ .



Point **T** is a distance  $2R$  from the surface.

What are the electric field strength and electric potential at **T**?

	Electric field strength	Electric potential
A	<del><math>\frac{E}{2}</math></del>	<del><math>\frac{V}{4}</math></del>
B	<del><math>\frac{E}{3}</math></del>	<del><math>\frac{V}{9}</math></del>
C	<del><math>\frac{E}{4}</math></del>	<del><math>\frac{V}{2}</math></del>
<u>D</u>	$\frac{E}{9}$	$\frac{V}{3}$

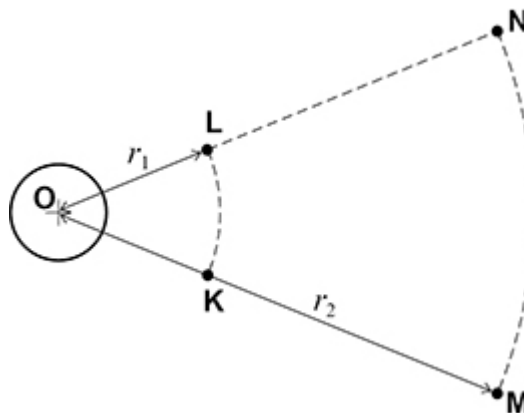


$$E \propto \frac{1}{r^2} \quad \therefore \frac{E}{3^2} = \frac{E}{9}$$

$$V \propto \frac{1}{r} \quad \therefore \frac{V}{3} = \frac{V}{3}$$

(Total 1 mark)

21. **O** is the centre of a negatively charged sphere.



**K** and **L** are two points at a distance  $r_1$  from **O**.  
**M** and **N** are two points at a distance  $r_2$  from **O**.

Which statement is true?

- A The work done moving an electron from **M** to **K** is the same as that done moving an electron from **K** to **L**.
- B The work done moving a positron from **K** to **M** is the same as that done moving an electron from **K** to **M**.
- C No work is done moving an electron from **M** to **N**.
- D No work is done moving a positron from **L** to **N**.

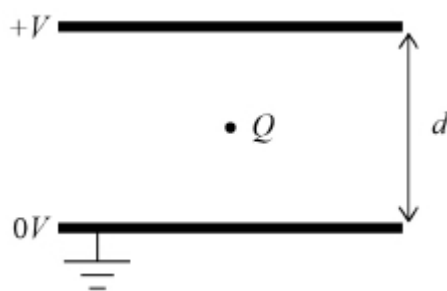
$$\Delta W = Q \Delta V$$

$$\text{but } \Delta V = 0$$

(Total 1 mark)

22.

A small object of mass  $m$  has a charge  $Q$ . The object remains stationary in an evacuated space between two horizontal plates. The plates are separated by a distance  $d$  and the potential difference between the plates is  $V$ .



What is  $V$ ?

- A  $\frac{mQg}{d}$
- B  $\frac{mdg}{Q}$
- C  $\frac{mQ}{d}$
- D  $\frac{md}{Q}$

$$V = \frac{E_p}{Q} = \frac{mgh}{Q} \quad \leftarrow h = d$$

$$V = \frac{mgd}{Q}$$

(Total 1 mark)

23. 1.5 mJ of work is done when a charge of 30  $\mu\text{C}$  is moved between two points, **M** and **N**, in an electric field.

What is the potential difference between **M** and **N**?

A 20 mV

B 20 V

C 45 V

D 50 V

$$\Delta V = \frac{\Delta W}{Q} = \frac{1.5 \times 10^{-3}}{30 \times 10^{-6}} = 50\text{V}$$

(Total 1 mark)

24. A parallel-plate capacitor is fully charged and then disconnected from the power supply. A dielectric is then inserted between the plates.

Which row correctly identifies the charge on the plates and the electric field strength between the plates?

	Charge	Electric field strength	
A	Stays the same	Increases	<input type="radio"/>
B	Increases	Decreases	<input type="radio"/>
C	Increases	Increases	<input type="radio"/>
<u>D</u>	Stays the same	Decreases	<input checked="" type="radio"/>

(Total 1 mark)

Dielectric reduces the electric field between the two charged plates, but does not change the charge.