

- M1.(a)** (i) Distance travelled in muons' frame of reference
 $= 10700(1-0.996^2)^{1/2} = 956 \text{ m}$ ✓
 Time taken in muons' frame of reference = $3.2 \mu\text{s}$ ✓
 This is 2 half-lives so number reaching Earth = 250 ✓
OR
 Time in Earth frame of reference
 $= 10700 / (0.996 \times 3 \times 10^8) = 3.581 \times 10^{-5} \text{ s}$ ✓
 Time taken in muons' frame of reference = $3.2 \mu\text{s}$ ✓
 This is 2 half-lives so number reaching Earth = 250 ✓
OR
 Half-life in Earth frame of reference
 $= 1.6 \times 10^{-6} / (1-0.996^2)^{1/2} = 17.9 \times 10^{-6} \text{ s}$ ✓
 Time taken = $35.8 \times 10^{-6} \text{ s}$ ✓
 This is 2 half lives so number reaching Earth = 250 ✓
OR
 Distance travelled in muons' frame of reference
 $= 10700(1-0.996^2)^{1/2} = 956 \text{ m}$ ✓
 Distance the muon travels in one half-life in muons reference frame
 $= 0.996 \times 3 \times 10^8 \times 1.6 \times 10^{-6} = 478 \text{ m}$ ✓
 Therefore 2 half-lives elapse to travel 956 m so number = 250 ✓
OR
 Decay constant in muon frame of reference
 Or decay constant in the Earth frame of reference ✓
 Uses the corresponding elapsed time and decay constant in
 $N = N_0 e^{-\lambda t}$ ✓
 Arrives at 250 ✓
All steps in the working must be seen
Award marks according to which route they appear to be taking
The number left must be deduced from the correct time that has elapsed in the frame of reference they are using

3

(ii)

	✓ if correct
For an observer in a laboratory on Earth the distance travelled by a muon is greater than the distance travelled by the muon in its frame of reference	✓
For an observer in a laboratory on Earth time passes more slowly than for a muon in its frame of	

reference	
For an observer in a laboratory on Earth, the probability of a muon decaying each second is lower than it is for a muon in its frame of reference	

1

- (b) (i) Total energy = $9.11 \times 10^{-31} \times (3 \times 10^8)^2 / (1-0.98^2)^{1/2}$ ✓
 4.12×10^{-13} J seen to 2 or more sf ✓
Show that so working must be seen

2

- (ii) Change = 7.5×10^{-14} J
 $V = 469$ (470) kV allow ecf using their answer to (i) ✓
ecf is their ((i) -3.37×10^{-13}) / 1.6×10^{-19}
Using 4×10^{-13} gives 394 (390) kV
Using 3.9×10^{-13} gives 331(330) kV
Do not allow 1 sf answer

1

[7]

- M2.(a)** speed of light in free space independent of motion of source and / or the observer ✓
and of motion of observer

1

- (b) laws of physics have the same form in all inertial frames
laws of physics unchanged from one inertial frame to another ✓

1

- (c) time taken(= $\frac{\text{distance}}{\text{speed}} = \frac{34 \text{ m}}{0.95 \times 3.0 \times 10^8 \text{ m s}^{-1}}$) = 1.2×10^{-7} s ✓

1

- (d) $t = \frac{18 \text{ ns}}{(1 - 0.95^2 c^2 / c^2)^{1/2}}$ ✓

Allow substitution for this mark

1

time taken for π meson to pass from one detector to the other = 58 ns ✓

1

2 half-lives (approximately) in the detectors' frame of reference. ✓

1

two half-lives corresponds to a reduction to 25 % so 75% of the π mesons passing the first detector do not reach the second detector. ✓

OR

Appreciation that in the lab frame of reference the time is about 6 half-lives had passed ✓

1

In 6 half-lives 1 / 64 left so about 90% should have decayed ✓

Clear conclusion made

Either Using special relativity gives agreement with experiment
or Failure to use relativity gives too many decaying (WTTE)

1

[8]

M3.(a) (A frame of reference) that has a constant velocity ✓

Accept no acceleration

1

(b) (i) Distance = 4.3 c light years (or 4.1×10^{16} m)

Correct answer only gets the mark

Speed (= $\frac{4.3 c}{5.0}$) = 2.6×10^8 m s⁻¹ (or 0.86 c)

Accept 2.58

1

(ii) $t = \left(\frac{t_0}{1 - v^2/c^2} \right)^{1/2}$ where $t = 5.0$ years (or 1.58×10^8 s)

and $v = 0.86 c$ (or $2.58 \times 10^8 \text{ m s}^{-1}$)

CF from bi to bii provided answer to bi

1st mark for correct substitution of either t or v into the above eqn ✓

$$t_o = 5.0 \times (1 - (0.86c)^2 / c^2)^{1/2} \checkmark = 2.6 \text{ years } \checkmark$$

Accept t or v in alternative units

Accept 1.58 (or 1.6) $\times 10^8 \text{ s}$ in place of 5.0 yr in 3rd mark point

Alt scheme

$l = l_o (1 - v^2 / c^2)^{1/2}$ where $t = 5.0 \text{ years}$ (or $1.58 \times 10^8 \text{ s}$) and $v = 0.86 c$ (or $2.58 \times 10^8 \text{ m s}^{-1}$)

Accept 2.5 to 2.6 to any number of sfs

1st mark for correct substitution of either t or v into the above eqn ✓

$$(l_o = 4.3 \times 365 \times 24 \times 3600 \times 3.0 \times 10^8 = 4.07 \times 10^{16} \text{ m})$$

$$l = 4.07 \times 10^{16} (1 - (0.86c)^2 / c^2)^{1/2} \text{ or } 2.08 \times 10^{16} \text{ m } \checkmark$$

$$t_o = \frac{l}{v} \left(= \frac{2.08 \times 10^{16} \text{ m}}{2.6 \times 10^8 \text{ m/s}} = 8.05 \times 10^7 \text{ s} \right) = 2.6 \text{ years } \checkmark$$

Alternative for last 2 marks in Alt scheme ($l_o = 4.3 \text{ l yr}$)

$$l = 4.3 (1 - (0.86c)^2 / c^2)^{1/2} = 2.2 \text{ l yr } \checkmark$$

$$t_o = \frac{l}{v} \left(= \frac{2.2}{0.86} \right) = 2.6 \text{ years } \checkmark$$

3

[5]

- M4.** (a) c is the same, regardless of the speed of the light source or the observer **(1)**

1

- (b) distance between detectors in rest frame of particles
(= $25 \times (1 - 0.98^2)^{1/2}$) = 5.0 m **(1)**

$$\text{time taken in rest frame of particles } \left(= \frac{\text{distance}}{\text{speed}} = \frac{5.0}{0.98c} \right) = 1.7 \times 10^{-8} \text{ s } \text{ (1)}$$

time taken to decrease by $\frac{1}{4}$ = 2 half lives **(1)**

$$\text{half life } (= 1.7 \times 10^{-8} / 2) = 8.5 \times 10^{-9} \text{ s } \text{ (1)}$$

[alternatively

time taken in rest frame of detectors $\left(= \frac{\text{distance}}{\text{speed}} = \frac{25.0}{0.98c} \right) = 8.5 \times 10^{-8} \text{ s}$
time taken in rest frame of particles
 $(= 8.5 \times 10^{-8} \times (1 - 0.98^2)^{1/2}) = 1.7 \times 10^{-8} \text{ s}]$

4

[5]

M5. (a) $10m_0 = m_0 \left(1 - \frac{v^2}{c^2} \right)^{-\frac{1}{2}}$ **(1)**

gives $\frac{v^2}{c^2} = 1 - 0.01 = 0.99$ **(1)**

$v = 0.995c = 2.98(5) \times 10^8 \text{ m s}^{-1}$ **(1)**

3

(b) $m = m_0 \left(1 - \frac{v^2}{c^2} \right)^{-\frac{1}{2}}$ **(1)**

$m \rightarrow \text{infinity as } v \rightarrow c$ **(1)**

[or m increases as v increases]

$E_k (= mc^2 - m_0c^2) \rightarrow \text{infinity as } v \rightarrow c$ **(1)**

$v = c$ would require infinite E_k (or mass) which is (physically)

impossible **(1)**

Max 3

[6]